Ś

Angle-resolved specific heat in iron-based superconductors: The case for a nodeless extended *s*-wave gap

A. V. Chubukov¹ and I. Eremin^{2,*}

¹Department of Physics, University of Wisconsin–Madison, Madison, Wisconsin 53706, USA ²Institut für Theoretische Physik III, Ruhr-Universität Bochum, D-44801 Bochum, Germany

(Received 15 June 2010; published 6 August 2010)

We consider the variation in the field-induced component of the specific heat $C(\mathbf{H})$ with the direction of the applied field in Fe pnictides within quasiclassical Doppler-shift approximation with special emphasis to recent experiments on FeSe_{0.4}Te_{0.6}. We show that for extended *s*-wave gap with no nodes, $C(\mathbf{H})$ has $\cos 4\phi$ component, where ϕ is the angle between **H** and the direction between hole and electron Fermi surfaces. The maxima of $C(\mathbf{H})$ are at $\pi/4$, $3\pi/4$, etc., if the applied field is smaller than $H_0 \leq 1$ T, and at $\phi=0$, $\pi/2$, etc., if the applied field is larger than H_0 . The angle dependence of $C(\mathbf{H})$, the positions of the maxima, and the relative magnitude of the oscillating component are consistent with the experiments performed in the field of 9 T $\geq H_0$. We show that the observed $\cos 4\phi$ variation does not hold if the *s*-wave gap has accidental nodes along the two electron Fermi surfaces.

DOI: 10.1103/PhysRevB.82.060504

PACS number(s): 74.20.Rp, 74.70.Xa, 74.25.Bt

The symmetry and the structure of the superconducting gap in Fe-based superconductors have been subjects of numerous experimental and theoretical papers in recent years.^{1–5} There is a growing consensus among researchers that the gap has an extended *s*-wave symmetry—it belongs to a symmetric A_{1g} representation of the D_{4h} symmetry group of a square lattice and its average values along electron and hole Fermi surfaces (FSs) are of opposite signs. It was argued by several groups^{2–5} that superconductivity originates from umklapp process in which pairs of fermions hop between conduction and valence bands, and that the pairhopping interaction is a combination of a screened Coulomb interaction and a magnetic interaction mediated by spin fluctuations.

A more subtle and currently hotly debated issue is whether the gap has nodes. This is not a symmetry issue as, quite generally, extended s-wave gap can be approximated by a constant only along the hole FS, while along the two electron FSs it has angle independent and $\cos 2\psi$ components: $\Delta_{e}(\psi) = \Delta_{e}(1 \pm b \cos 2\psi)$, where ψ is the angle counted from the line connecting the two FSs and the sign of Δ_e is opposite to the sign of the gap along hole FSs. Such $\Delta_e(\psi)$ has no nodes if b < 1 and has "accidental" nodes when b > 1 at nonsymmetry selected directions $\cos 2\psi = 1/b$ Because Fe pnictides are multiorbital systems, the $\cos 2\psi$ component of the interaction is generally not small, i.e., b can be either larger or smaller than 1, depending on the material. Furthermore, b gets larger when one includes into the gap equation intraband Coulomb repulsion because this term couples to the gap averaged over the FS and hence reduces angle-independent gap components but does not affect $\cos 2\psi$ components (see second reference in Ref. 4). As a consequence, b becomes progressively larger as the system moves further away from the spin-density wave phase and the effect of intraband repulsion grows, that is, overdoped ferropnictides are more likely to have nodes in the gap.

The issue whether or not the gap in Fe pnictides has nodes is crucial for the understanding of low-energy properties of these materials and deserves a careful study. The subject of this work is the interpretation of recent high-accuracy measurements⁶ of the dependence of the low-temperature specific heat in $FeSe_{0.4}Te_{0.6}$ on the direction of a magnetic field. Similar experiments have been carried out in the past on borocarbides,⁷ and heavy-fermion CeCoIn₅ (Ref. 8) and revealed modulations generally consistent with the *d*-wave gap (for details see Refs. 9–12; for experiments on thermal conductivity see Ref. 13).

The generic reason for field-induced modulations of specific heat and thermal conductivity in unconventional superconductors is that a magnetic field induces vortices along the field direction. In a vortex state of a type-II superconductor, scattering of quasiparticles on vortices gives rise to a nonzero density of states (DOS) at zero energy. The magnitude of this residual DOS depends on the angle the field makes with the position of the minima of the modulus of the superconducting gap. This leads to modulations of the fieldinduced linear-in-T term in the specific heat.9,10,14 This reasoning works the best when the gap has nodes but should be generally applicable also to materials where the gap varies along the FS but not necessary has nodes, provided that the field is not too small. Fe pnictides are strong type-II superconductors [both magnetic and coherence lengths are of order $2-3 \times 10^2$ Å, much smaller than the penetration depth $\lambda\!\sim\!3\!\times\!10^3$ Å (Ref. 15)] and vortex state extends to almost all fields [the upper critical field is about 100 T, lower critical field is about $H_{c1} \leq 10 \text{ mT}$ (Ref. 16)].

In FeSe_{0.4}Te_{0.6}, the data⁶ show cos 4 ϕ modulation of $C(\mathbf{H})$, with the magnitude of about 1% of the total field induced $C(\mathbf{H})$. The maximum of $C(\mathbf{H})$ is at $\phi=0$, $\pi/2$, etc., what correspond to the directions of **H** along the axis between hole and one of electron FSs in the unfolded Brillouin zone (BZ) (along the diagonals in the folded BZ). The cos 4 ϕ modulation of $C(\mathbf{H})$ was originally interpreted⁶ as evidence for the nodes in the gap. However, to be consistent with the observed near-perfect cos 4 ϕ form of $C(\mathbf{H})$, the nodes have to be located precisely at 45° with respect to the *x* axis, i.e., right at the crossing points of two electron FSs in the folded BZ (see Fig. 1). This is generally incompatible



FIG. 1. (Color online) Fermi-surface topology of iron-based superconductors in the (a) unfolded and (b) folded BZ. There are two small hole pockets centered around the Γ point and two elliptic electron pockets centered around the $(\pm \pi, 0)$ point and $(0, \pm \pi)$ point of the unfolded BZ. Upon folding two electron pockets fold into the (π, π) point of the folded BZ [dashed-dotted line in (a) is the boundary of the folded BZ]. The magnetic field rotation is shown by angle ϕ_0 .

with the "accidental" nodes located at some arbitrary angles ϕ . The authors of Ref. 6 argued that the data are inconsistent with no-nodal extended *s*-wave gap and an extended *s*-wave gap with accidental nodes. To explain the data, they included spin-orbit coupling and argued that it creates nodes on electron FSs at exactly 45°, even if the gap was nodeless in the absence of spin-orbit interaction.⁶

In this Rapid Communication, we argue that the data of Ref. 6 can be actually explained *quantitatively* in a conventional semiclassical Doppler-shift scenario for field-induced oscillations of $C(\mathbf{H})$, but only if one assumes that the gaps along the electron FSs have no nodes. The nodeless gap in FeSe_{0.4}Te_{0.6} has been extracted from scanning tunnel microscope (STM) data¹⁷ and we argue that STM and angle-resolved specific-heat measurements are consistent with each other.

Our reasoning is twofold: first, as we said, the two electronic gaps generally have the forms $\Delta_e = \Delta(1 \pm b \cos 2\psi)$. The formula for the specific heat⁹ contains Δ_{e}^{2} , i.e., $\cos 2\psi$ and $\cos 4\psi$ terms. The $\cos 2\psi$ terms cancel out when the contributions from the two electron FSs are added while the $\cos 4\psi$ term generates $\cos 4\phi$ modulation of $C(\mathbf{H})$. This, however, holds only if Δ_e does not have nodes (b < 1), otherwise the modulation of $|\Delta_e|$ will be more complex leading to a more complex structure of $C(\mathbf{H})$. Second, we show that the sign of the cos 4ϕ modulation depends on the ratio $a^2 = \frac{\Delta^2 \Lambda^2}{v_F^2} = \frac{H_0}{H}$, where v_F is the Fermi velocity for the electron pocket and $\Lambda = \sqrt{\hbar c/(2|e|H)}$ is the magnetic length, and changes from negative to positive as the field increases. We estimated the field where the sign changes and found that for $v_F \approx 3.3 \times 10^5$ m/s (Ref. 6) it is about 1 T for all b < 1, much smaller than 9 T, at which experiments have been performed. This implies that $\cos 4\phi$ oscillations of $C(\mathbf{H})$ at the field of 9 T have maxima at $\phi=0, \pi/2$, in agreement with the data. [We caution, however, that the field at which the sign of $\cos 4\phi$ component in $C(\mathbf{H})$ changes would be larger if the value of v_F was smaller than the one we used]. We also found that at 9 T field, the magnitude of the oscillating part of $C(\mathbf{H})$ is around 1% of the total specific heat, like in the data,⁶ and this number weakly depends on b except for very small values, where it vanishes as b^2 . The conclusion of our analysis is that the data on $C(\mathbf{H})$ are quite consistent with the "conventional" theory of field-induced oscillations, provided that the gaps along electron FSs have moderate $\cos 2\psi$ oscillations and no nodes.

The range $b \approx 1$ is a gray area, and in the presence of some amount of disorder modulations of $C(\mathbf{H})$ may still look like $\cos 4\phi$ even when the gap has pairs of weakly spaced "accidental" nodes. Still, a more natural explanation of the data in FeSe_{0.4}Te_{0.6} is that the gap has no nodes.

The sign change in the prefactor for the oscillating $\cos 4\phi$ component in the specific heat and thermal conductivity is the well-known phenomenon for *d*-wave superconductors. The detailed theoretical study of the sign variation in the prefactor for the $\cos 4\phi$ term with changing magnetic field and temperature has been performed by Vorontsov and Vekhter (VV) (Ref. 9) and by Hiragi *et al.*¹⁰ VV recently performed numerical analysis of the angular dependence of $C(\mathbf{H})$ in the ferropnictides¹⁸ and found the change from negative to positive prefactor of the $\cos 4\phi$ term with increasing field and temperature. Our results are fully consistent with theirs and provide analytical reasoning for the sign change in the $\cos 4\phi$ term in the iron-based superconductors.

The specific heat is expressed via the density of states as

$$C(T,\mathbf{H}) = \frac{1}{2} \int_{-\infty}^{+\infty} d\omega \frac{\omega^2 N(T,\mathbf{H};\omega)}{T^2 \cosh^2(\omega/2T)},$$
$$N(T,\mathbf{H};\omega) = \int_{0}^{2\pi} \frac{d\psi}{2\pi} \sum_{i} N_{\psi}^{i}(T,\mathbf{H};\omega),$$
(1)

where *j* is the band index. The scattering of quasiparticles on vortices gives rise to a finite DOS at zero energy what in turn for $T \rightarrow 0$ yields $C(T, \mathbf{H}) \approx AN(0, \mathbf{H}; \omega)T$ with some constant *A* and $N(0, \mathbf{H}; \omega)$ is a density of states at zero temperatures. The experiment⁶ has been performed at low enough $T \sim 2.6$ K when terms of higher order in *T* are irrelevant.

We consider FS geometry consisting of two hole FSs centered at Γ point and two electron FSs centered at $(0, \pi)$ and $(\pi, 0)$ in the unfolded BZ, or at (π, π) in the folded BZ (Fig. 1). The potential presence of the third hole FS is not essential for our analysis because oscillations of $C(\mathbf{H})$ come only from the two electron bands. For simplicity, we assume that all bands are circular, i.e., neglect ellipticity of electron bands. We will follow Ref. 9 and employ the formula for $N^{j}(\mathbf{H}, \psi)$ obtained by solving semiclassical Eilenberger equations for a given vortex lattice within Brandt-Pesch-Tewordt (BPT) approximation in which the dependence on the normal Green's function on the center-of-mass coordinate of a pair is replaced by an average over a unit cell of the vortex lattice. Hiragi et al.¹⁰ computed the DOS beyond BPT approximation and found that the corrections to the BPT are quite small. Suppose that **H** is applied in Fe-Fe plane, at an angle ϕ with respect to the x axis (which in momentum space is the direction between hole and electron bands). In the area surrounding the vortex, the DOS at zero energy can be generally written as^{6,9,14}



FIG. 2. (Color online) Calculated angular dependence of the density of states for (a) large a=10 and (b) small a=0.1. We set b=0.5. The solid and dashed curves refer to the numerical solution of Eq. (3) and the approximate analytical formulas (4) and (5), respectively. In panel (a) we matched analytical and numerical curves at $\phi=0$.

$$N^{j}(\mathbf{H}, \psi) = \frac{\alpha(\mathbf{H}, \psi)}{\sqrt{\alpha^{2}(\mathbf{H}, \psi) + [\Delta^{j}(\psi)]^{2}}},$$
(2)

where $\alpha(\mathbf{H}, \psi)$ is proportional to the Fermi velocity component normal to the field $v_F^{\perp} = v_F \sin(\psi - \phi)$: $\alpha(\mathbf{H}, \phi) = \overline{\alpha} \sin(\psi - \phi)$, where $\overline{\alpha} = cv_F/(2\sqrt{2}\Lambda)$, Λ is the magnetic length, and c=O(1) is a numerical factor which contains information about the geometry of the vortex structure and the distance from the vortex core.⁶

Substituting $\Delta_e = \Delta(1 \pm b \cos 2\psi)$ and $\Delta_h = \text{const into Eq.}$ (2) and shifting the integration variable, we obtain $N(\mathbf{H})$ $=N_h(H)+N_e(\mathbf{H})$, where N_h is independent on the direction of **H**, and $N_e(\mathbf{H}) = \int_0^{2\pi} \frac{d\psi}{2\pi} [N_e(\mathbf{H}, \psi)] + N_e(\mathbf{H}, \psi + \pi/2)$, where

$$N_e(\mathbf{H}, \psi) = \sqrt{\frac{1}{1 + \frac{a^2 [1 + b \cos(2\psi + 2\phi)]^2}{\sin^2 \psi}}}$$
(3)

and we remind that $a^2 = \frac{\Delta^2}{a^2} = H_0/H$. Consider the limits of small and large *a* separately. At large a (small fields) $N_e(\mathbf{H}) \propto 1/a$. Oscillating component of N_e can be obtained analytically at small b. Expanding in b we find

$$N_e(\mathbf{H}) = N_e(H) - \frac{2b^2}{15\pi|a|}\cos 4\phi + O(b^4), \tag{4}$$

where $N_e(H)$ is a *b*-dependent nonoscillating term. We see that the DOS does contain $\cos 4\phi$ oscillations, as we anticipated, however the sign of the $\cos 4\phi$ term is negative, which implies that $C(\mathbf{H})$ has peaks at $\pi/4$, $3\pi/4$, etc., in disagreement with the data. At larger b, the oscillating part of $N_{e}(\mathbf{H})$ contains higher harmonics $\cos 8\phi, \cos 12\phi, \ldots$ and has to be calculated numerically. We present the results in Fig. 2(a). We see that the oscillating part of $N_e(\mathbf{H})$ still well described by $\cos 4\phi$ form for arbitrary b < 1, despite that higher harmonics are not parametrically small. Also, the sign of the oscillating part remains negative at large a for arbitrary b < 1 [i.e., for all b < 1, the maxima of $C(\mathbf{H})$ are at $\pi/4$, etc.].

The situation changes, however, in the opposite limit of large fields, when $a \leq 1$. Now $N_e(\mathbf{H})$ can be expanded in a. The expansion requires care because of infrared divergencies and yields, at arbitrary b < 1,

PHYSICAL REVIEW B 82, 060504(R) (2010)



FIG. 3. (Color online) (a) The functional form of the function $a^{2}F(a)$ from Eqs. (6) and (7). Sign change in F(a) implies sign change in the prefactor for $\cos 4\phi$ term in the density of states; (b) the difference between $N(\phi)$ for $\phi = \pi/2$ and $\phi = \pi/4$ from Eq. (3) as a function of a for various b. For any b from the interval 0 < b $<1, N(\pi/2)-N(\pi/4)$ changes sign at a finite $a=a_0$, ranging between 0.65 and 2.8.

$$N_e(\mathbf{H}) = 2 - \frac{4a}{\pi} + 2a^2b^2\cos 4\phi[1+O(a)] + \cdots, \quad (5)$$

where dots stand for terms of order a^4 , at which order higher harmonics appear. We see that the oscillating component is now $\cos 4\phi$ for all b < 1, and the sign of the oscillating part is positive, i.e., the maxima of $C(\mathbf{H})$ are now at ϕ =0, $\pi/2,...$, like in the experimental data.⁶ In Fig. 2(b) we present the result of numerical evaluation of $N_e(\mathbf{H})$ and compare it with Eq. (5). Clearly, there are $\cos 4\phi$ oscillations with a positive prefactor.

The value of a at which the oscillating part of $N_e(\mathbf{H})$ changes sign, and the crossover from a small field to a highfield behavior can be analyzed analytically at small b. Expanding Eq. (3) in b to order b^2 and integrating over ψ we obtain

$$N_e(\mathbf{H}) = \frac{4}{\pi} \arctan \frac{1}{a} + a^2 b^2 \cos 4\phi F(a),$$
 (6)

where

$$F(a) = \frac{1}{2\pi} \int_0^{\pi} d\psi \frac{\sin\psi\cos 4\psi}{(a^2 + \sin^2\psi)^{5/2}} (2a^2 - \sin^2\psi).$$
(7)

We plot $a^2F(a)$ in Fig. 3(a). This function changes sign at $a=a_0 \approx 0.65$ and is negative at larger a (smaller fields). The implication of this result is that $C(\mathbf{H})$ changes sign at a *finite* field even when the gap anisotropy is infinitesimally small. We analyzed the evolution of a_0 with increasing b and found [Fig. 3(b)] that a_0 remains finite and of order 1 for all b < 1. Observe also that $a^2 F(a)$ is of order 10^{-2} for all a except for the smallest one, i.e., for $b \sim 1$, the oscillating part of $C(\mathbf{H})$ is of order 10^{-2} of the total $C(\mathbf{H})$.

In Fig. 4 we present $N_{e}(\mathbf{H})$ for b > 1, when the gap along electron FSs has accidental nodes at $\cos 2\psi = 1/b$. We clearly see that the angular dependence is different from $\cos 4\phi$ —there appear additional maxima or minima in $N_e(\mathbf{H})$ associated with zeros of Δ_e (minima of $|\Delta_e|$). These deviations from $\cos 4\phi$ form for b > 1 have been reported before.¹⁹

To estimate the value of H_0 in $a=H_0/H$, we use Λ ≈ 180 Å/ \sqrt{B} , where B is the value of a field in tesla, and take $v_F \sim 3.3 \times 10^5$ m/s, averaged between two electron



FIG. 4. (Color online) The angular dependence of the density of states, Eq. (3), for b > 1. The form of $N(\phi, H)$ is clearly different from $\cos 4\phi$. Additional minima or maxima correspond to the nodes at $\cos 2\psi = 1/b$. Panel (a)—large fields, a < 1, panel (b)—small fields, a > 1. The sign of the oscillating component still depends on whether or not *a* exceeds some *b*-dependent critical value.

bands,⁶ and $\Delta_e \sim 4$ meV.²⁰⁻²² We obtain $H_0 = (0.89/c^2)$ T. Hanaguru et al.¹⁷ extracted a smaller $\Delta \sim 1.7$ meV from their STM data. This will lead to even smaller H_0 $\sim (0.16/c^2)$. The value of c is not known but should generally be of order 1. For $c \leq 1$, H_0 is well below 9 T at which the experiments are performed. In other words, H=9 T is deep inside the range of $H > H_0$, when the oscillating part of $C(\mathbf{H})$ has $\cos 4\phi$ form with the maxima at $\phi=0, \pi/2$, etc. Using $H_0 \sim 1$ T for definiteness and collecting the contributions to $N(\mathbf{H})$ from two hole and two electron bands, we found that the amplitude of the oscillating part of $C(\mathbf{H})$ is $0.028(2b)^2$ of the total $C(\mathbf{H})$, which for 2b = O(1) is quite consistent with 1% effect observed in the experiment.⁶ We caution, however, that $H_0 \le 1$ T is obtained using $v_F \sim 3.3$ $\times 10^5$ m/s taken from Ref. 6. Smaller values of $\leq 10^5$ m/s have been reported for $Ba_{0.6}K_{0.4}Fe_2As_2$.²³ If v_F is smaller, $H_0 \propto 1/v_F^2$ can be larger than 9 T.

To conclude, we considered analytically, within BPT ap-

- *On leave from Kazan State University, 420008 Kazan, Russian Federation.
- ¹Y. Kamihara *et al.*, J. Am. Chem. Soc. **130**, 3296 (2008).
- ²I. I. Mazin *et al.*, Phys. Rev. Lett. **101**, 057003 (2008); K. Kuroki *et al.*, *ibid.* **101**, 087004 (2008); V. Barzykin and L. P. Gorkov, JETP Lett. **88**, 131 (2008).
- ³S. Graser *et al.*, New J. Phys. **11**, 025016 (2009); T. A. Maier *et al.*, Phys. Rev. B **79**, 224510 (2009).
- ⁴A. V. Chubukov *et al.*, Phys. Rev. B **78**, 134512 (2008); A. V. Chubukov *et al.*, *ibid.* **80**, 140515(R) (2009); A. V. Chubukov, Physica C **469**, 640 (2009); V. Cvetkovic and Z. Tesanovic, EPL **85**, 37002 (2009); V. Stanev *et al.*, Phys. Rev. B **78**, 184509 (2008).
- ⁵ Fa Wang *et al.*, Phys. Rev. Lett. **102**, 047005 (2009); Fa Wang *et al.*, Phys. Rev. B **81**, 184512 (2010); C. Platt, C. Honerkamp, and W. Hanke, New J. Phys. **11**, 055058 (2009); R. Thomale *et al.*, Phys. Rev. B **80**, 180505 (2009); V. Stanev *et al.*, arXiv:1006.0447 (unpublished).
- ⁶B. Zeng et al., arXiv:1004.2236 (unpublished).
- ⁷T. Park *et al.*, Phys. Rev. Lett. **92**, 237002 (2004).
- ⁸H. Aoki et al., J. Phys.: Condens. Matter 16, L13 (2004).
- ⁹A. B. Vorontsov and I. Vekhter, Phys. Rev. Lett. **96**, 237001 (2006); Phys. Rev. B **75**, 224501 (2007).

PHYSICAL REVIEW B 82, 060504(R) (2010)

RAPID COMMUNICATIONS

proximation, the variation in the field-induced component of the specific heat with the direction of the applied field. We demonstrated that this scenario yields the $\cos 4\phi$ variation with the maxima at $\pi/4$, $3\pi/4$, etc., if the applied field is smaller than $H_0 \leq 1$ T, and $\cos 4\phi$ variation with the maxima at $\phi=0, \pi/2$, etc., if the applied field is larger than H_0 . Both results are valid provided that the gaps along electron FSs have $\cos 2\psi$ component but no nodes. We argued that the $\cos 4\phi$ form of oscillating part, the positions of the maxima, and the relative magnitude of the oscillating component of $C(\mathbf{H})$ are consistent with the experiments by Zheng *et al.*⁶ performed in the 9 T field, well above H_0 . We therefore argue that the data on the angular dependence of field-induced $C(\mathbf{H})$ in $\text{FeSe}_{0.4}\text{Te}_{0.6}$ are actually consistent with no-nodal extended s-wave gap in this material. The same no-nodal extended s-wave gap has been extracted from STM,¹⁷ Andreev reflection,²¹ and optical conductivity²² data on FeSe_{0.45}Te_{0.55}.

Note added in proof. Recent results by the authors of Ref. 24 show that the oscillating part of $C(\mathbf{H})$ at H=9 T changes sign with increasing T. Our results are consistent with experiment at a higher T=3.7 K. According to Ref. 18, the behavior at higher T and higher H are the same, and at high enough T, the sign of oscillations is the same as in our work for all T. The observed sign change most likely indicates that H_0 is close to 9 T.

We thank C. Homes, I. Mazin, H.-H. Wen, and particularly A. Vorontsov for useful conversations. A.V.C. acknowledges the support from Grant No. NSF-DMR 0906953 and AvH Foundation. I.E. acknowledges the support from the RMES Program (Contract No. N 2.1.1/2985). A.V.C. is thankful to MPIPKS in Dresden for hospitality during the work on the manuscript.

- ¹⁰M. Hiragi et al., arXiv:1004.2332 (unpublished).
- ¹¹G. R. Boyd *et al.*, Phys. Rev. B **79**, 064525 (2009); Y. Nagai and N. Hayashi, Phys. Rev. Lett. **101**, 097001 (2008).
- ¹²P. Miranović et al., Phys. Rev. B 68, 052501 (2003).
- ¹³Y. Matsuda et al., J. Phys.: Condens. Matter 18, R705 (2006).
- ¹⁴S. K. Yip and J. A. Sauls, Phys. Rev. Lett. **69**, 2264 (1992); G. E. Volovik, JETP Lett. **58**, 469 (1993); D. Xu *et al.*, Phys. Rev. B **51**, 16233 (1995); I. Vekhter *et al.*, *ibid.* **59**, R9023 (1999); I. Vekhter *et al.*, *ibid.* **64**, 064513 (2001).
- ¹⁵R. Prozorov et al., Physica C 469, 667 (2009).
- ¹⁶H. Kim *et al.*, arXiv:1001.2042 (unpublished).
- ¹⁷T. Hanaguri *et al.*, Science **328**, 474 (2010).
- ¹⁸A. Vorontsov and I. Vekhter, arXiv:1006.0738 (unpublished). Note that the definition of the angle ϕ in this work (and in the latest version of Ref. 6) differs from ours by 45°.
- ¹⁹S. Graser et al., Phys. Rev. B 77, 180514(R) (2008).
- ²⁰K. Nakayama et al., arXiv:0907.0763 (unpublished).
- ²¹W. Park et al., arXiv:1005.0190 (unpublished).
- ²²C. C. Homes *et al.*, Phys. Rev. B **81**, 180508 (2010). This work reported two gaps, $\Delta = 4$ meV which we used is close to the average between the two.
- ²³H. Ding et al., arXiv:0812.0534 (unpublished).
- ²⁴B. Zeng et al., arXiv:1007.3597 (unpublished).